## Letters to the Editor

## **PROTON-PROTON SCATTERING IN THE** $^{1}D_{2}$ STATE AT 616 Mev

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PRODUCTION of  $\pi$  mesons in p-p collisions, which proceeds rather intensively beginning with proton energies of ~400 Mev, complicates substantially the character of the elastic scattering. The connection between elastic and inelastic scattering is analyzed with the aid of the unitarity of the S matrix. In the region of proton energies of ~600 Mev, the initial <sup>1</sup>D<sub>2</sub> state of the two protons plays an essential role.

If we consider only processes with the production of a single  $\pi$  meson, and also neglect dstates of the  $\pi$  meson, then the following processes can go through the  ${}^{1}D_{2}$  state: (1) elastic p-p scattering; (2) the transition  ${}^{1}D_{2} \rightarrow ({}^{3}S_{1}p)_{2}$ in the reaction  $p+p \rightarrow d + \pi^{+}$ ; (3) the transition  ${}^{1}D_{2} \rightarrow ({}^{3}S_{1}p)_{2}$  in the reaction  $p + p \rightarrow n + p + \pi^{+}$ ; (4) the transition  ${}^{1}D_{2} \rightarrow ({}^{3}P_{2}s)_{2}$  in the reaction  $p + p \rightarrow \pi^{0} + p + p$ .

The probability of emission of  $\pi^0$  meson in an s state is rather low, since process (4) is negligible in the energy region considered. Then the S matrix for the initial  ${}^1D_2$  state (T = 1; J = 2; II = +) can be written

$$S = \begin{pmatrix} S_{11} & iS_{12} & iS_{13} \\ -iS_{12} & S_{22} & S_{23} \\ -iS_{13} & S_{23} & S_{33} \end{pmatrix},$$

where the suffix 1 denotes the p-p system, 2 the  $(\pi^+d)$  system, and 3 the  $(\pi^+np)$  system.

The values of  $|S_{12}|^2$  and  $|S_{13}|^2$  can be determined using the results of references 1 and 2 and also of reference 3. For the energy  $E_p = 654$  MeV we obtain  $|S_{12}|^2 = 0.31$  and  $|S_{13}|^2 = 0.41$ . Then, using one of the unitarity conditions  $|S_{11}|^{2*} + |S_{12}|^2$ 



Dependence of the squares of S-matrix elements on proton energy. O - results of reference 1.

+  $|S_{13}|^2 = 1$ , we find  $|S_{11}|^2 = 0.28$ . In the figure we show the data for a wide range of  $E_p$ , from 400 to 800 Mev. It can be seen from the graph that all three curves have the tendency to go through the same point at a proton energy of  $E_p = 616$  Mev, which has the feature that the total energy of two colliding protons<sup>4</sup> in the center-of-mass system is equal to the resonance energy for meson-nucleon scattering, when account is taken of the  $\pi$ -meson rest mass.

If we assume that this, in fact, occurs, then the remaining two unitarity relations give

$$|S_{22}|^2 = |S_{33}|^2; |S_{22}|^2 + |S_{23}|^2 = 2/3.$$

These results can be used in carrying out phaseshift analyses of p-p scattering and scattering  $\pi^+$ mesons on deuterons.

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<sup>1</sup>M. G. Meshcheriakov and B. S. Neganov, Dokl. Akad. Nauk SSSR 100, 677 (1955).

<sup>2</sup> Akimov, Savchenko and Soroko, J. Exptl. Theoret. Phys. **35**, 89 (1958), (this issue, p. 69).

<sup>3</sup>S. Mandelstam, Proc. Roy. Soc. A244, 491 (1958).

<sup>4</sup> Meshcheriakov, Neganov, Soroko and Vzorov, Dokl. Akad. Nauk SSSR **99**, 959 (1954).

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